Artificial Intelligence

Informed Search Chiến lược tìm kiếm kinh nghiệm

Informed (Heuristic) Search

- We have seen that uninformed methods of search are capable of systematically exploring the state space in finding a goal state.
- However, uninformed search methods are very inefficient in most cases.
- With the aid of problem-specific knowledge, informed methods of search are more efficient.

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Outline

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- Heuristics
- Informed Search methods:
 - Greedy Best-first search
 - Beam Search
 - Uniform-cost search
 - A* search

Heuristics

- "Heuristics are criteria, methods or principles for deciding which among several alternative courses of action promises to be the most effective in order to achieve some goal."
- Can make use of heuristics in deciding which is the most "promising" path to take during search.
- Evaluation function h(u): a measure to evaluate the *distance* of state u from the goal. e.g: h(u) = 0 if u is the goal state.
- Evaluation functions (or heuristic functions) are problem specific functions that provide an estimate of solution cost.

Evaluation Function Hàm đánh giá

 Travelling problem: The evaluation function take the value of the straightline from one city to the destination city.

Pham Bảo Sơn





- Eight-puzzle problem:
- The number of misplaced tiles, or
- Total sum of distances of a tile and its desired location.

- WAR	4	3	1	
A State		6	5	
	8	2	7	

1	2	3
8		4
7	6	5

- The number of misplaced tiles: 9

- Total sum of distances of a tile and its desired location: 3 + 1 + 2 + 1 + 1 + 1 + 2 + 2 = 14



- There are many ways to estimate the solution cost for an evaluation function.
- Evaluation functions might not be optimal.
- The quality of an evaluation function plays an important role in the effectiveness of the informed search.

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Informed Search

- 1. Task specification by identifying state space and actions.
- 2. Identify an evaluation function.
- 3. Design a strategy to choose which node to expand next.

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Greedy Best-First Search

- Tìm kiếm tốt nhất đầu tiên
- Best first Search that selects the next node for expansion using the evaluation function h(u).
- Greedy search minimises the estimated cost to the goal; it expands whichever node u that is estimated to be closest to the goal.

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Greedy best-first search example



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Greedy best-first search example





Greedy best-first search example



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Greedy best-first search example



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Greedy Best First Search

1. Initialize queue L containing only the initial state.

2. Loop do

- 2.1 **If** (L is empty) **then** {search failed; exit}
- 2.2 Take the first node u from beginning of L;
- 2.3 **If** (u is a goal) **then** {goal found; exit}
- 2.4 For (each node v adjacent to u) do {Put v to L so that L is sorted in increasing order
 - of the evaluation function}

Greedy Best first search



Properties of greedy bestfirst search

 <u>Complete</u>? No – can get stuck in loops, e.g., lasi → Neamt → lasi → Neamt →

Complete in finite space with repeated-state checking

- <u>Time?</u> O(b^m), m is the maximum depth in search space
- <u>Space?</u> O(b^m) -- keeps all nodes in memory
- Optimal? No

A good heuristic function can reduce time and memory cost substantially.

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- Similar to greed best first search but only consider expanding k nodes at the next step i.e. the queue has a maximal size of k.
- Pros: better time complexity
- Cons: do not consider all paths, so might fail to find a solution i.e. not complete.

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Uniform-Cost Search

- Expand root first, then expand least-cost unexpanded node.
- Implementation: insert nodes in order of increasing path cost.
- Reduces to breadth-first search when all actions have same cost.
- Find the cheapest goal provided path cost is monotonically increasing along each path (i.e. no negative-cost steps)

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Uniform Cost Search

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Properties of Uniform Cost Search

- <u>Complete?</u> Yes, if step cost >0 or b is finite
- <u>Time?</u> O(b^m), m is the maximum depth in search space
- <u>Space?</u> O(b^m) -- keeps all nodes in memory
- Optimal? Yes

Can we still guarantee optimality but search more efficiently, by giving priority to more promising nodes?

A* Search

- A* Search uses evaluation function f(n) = g(n) + h(n)
 - g(n): cost from initial node to node n
 - h(n): estimated cost of cheapest path from n to goal.
 - f(n): estimated total cost of cheapest solution through n.

- Greedy best first search minimises h(n)
 - Efficient but not optimal or complete
- Uniform-cost search minimizes g(n)
 - Optimal and complete but not efficient

A* Search

- A* search minimizes f(n) = g(n) + h(n)
 - Idea: preserve efficiency of Greedy Search but avoid expanding path that are already expensive
- Question: Is A* search optimal and complete?

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• Yes! Provided h(n) is *admissible*- it never overestimates the cost to reach the goal.



A* Search Example 118 Zerind Sbu Timisoara 393 Phạm Bảo Sơn 29



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A* Search

1. Initialize queue L containing only the initial state.

2. Loop do

- 2.1 If (L is empty) then {search failed; exit}
- 2.2 Take the first node u from beginning of L;
- 2.3 If (u is a goal) then {goal found; exit}
- 2.4 For (each node v adjacent to u) do

 ${g(v) := g(u) + k(u,v);}$

f(v) := g(v) + h(v);

Put v to L so that L is sorted in increasing order of the evaluation function f;}

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Admisible Heuristics

- Hàm đánh giá chấp nhận được
- An evaluation function h(n) is admissible if h(n) is always optimistic ("lac quan"): it never overestimates the optimal cost.
- If h(n) is admissible then A* is optimal.

Optimality of A* (proof)

• Suppose some suboptimal goal G_2 has been generated and is in the fringe. Let *n* be an unexpanded node in the fringe such that *n* is on a shortest path to an optimal goal *G*.



Optimality of A* Search

- Since f(G₂) > f(n), A* will never select G₂ for expansion.
- The suboptimal goal node G₂ may be *generated*, but it will never be *expanded*.
- In other words, even after a goal node has been generated, A* will keep searching so long as there is a possibility of finding a shorter solution.
- Once a goal node is selected for expansion, we know it must be optimal, so we can terminate the search.

Properties of A* search

- Complete? Yes (unless there are infinitely many nodes with f ≤ f(G))
- <u>Time?</u> Exponential
- <u>Space?</u> Keeps all nodes in memory

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Optimal? Yes

Admissible heuristics

E.g., for the 8-puzzle:

- $h_1(n)$ = number of misplaced tiles
- $h_2(n)$ = total Manhattan distance
- (i.e., no. of squares from desired location of each tile)



Start State

7 8

4

3

6

2

5

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Goal State

• $h_1(S) = ?$ • $h_2(S) = ?$

Admissible heuristics

E.g., for the 8-puzzle:

- $h_1(n)$ = number of misplaced tiles
- $h_2(n)$ = total Manhattan distance
- (i.e., no. of squares from desired location of each tile)





Goal State

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Start State

- $h_1(S) = ?8$
- $h_2(S) = ? 3 + 1 + 2 + 2 + 3 + 3 + 2 = 18$

Dominance Tính áp đảo

- If $h_2(n) \ge h_1(n)$ for all *n* (both admissible)
- then h_2 dominates h_1
- h_2 is better for search
- Typical search costs (average number of nodes expanded):

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• d=12

IDS = 3,644,035 nodes

A^*(h_1) = 227 nodes

A^*(h_2) = 73 nodes

• d=24

IDS = too many nodes ~ 54 * 10<sup>9</sup> nodes

A^*(h_1) = 39,135 nodes

A^*(h_2) = 1,641 nodes
```

Cách tìm admissible heuristics

- Giảm bớt ràng buộc.
- A problem with fewer restrictions on the actions is called a relaxed problem
- The cost of an optimal solution to a relaxed problem is an admissible heuristic for the original problem
- If the rules of the 8-puzzle are relaxed so that a tile can move anywhere, then $h_1(n)$ gives the shortest solution
- If the rules are relaxed so that a tile can move to any adjacent square, then h₂(n) gives the shortest solution

Composite Heuristic Functions

 Let h₁, h₂,.., h_m be admissible heuristics for a given task.

- Define the composite heuristic:
 - $h(n) = max (h_1(n), h_2(n), ..., h_m(n)).$
- h is admissible
- h dominates h₁, h₂, ..., h_m

Bidirectional Search

- Symmetrical problems.
- We can have inverse operators.
- Explicate goal states



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Properties of Bidirectional search

- <u>Complete?</u> Yes (if *b* is finite)
- <u>Time?</u> O(b^{d/2})
- <u>Space?</u> *O*(*b*^{*d*/2})
- Optimal? Yes (if uniform cost per step)

References

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- Al Illuminated. Chapter 4.